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## WHAT IS CLAIMED IS:

- A method of modeling the behavior of a molecule, comprising selecting a torsion angle, rigid multibody model for said molecule, said model having equations of motion;
- selecting an implicit integrator; and
  generating an analytic Jacobian for said implicit integrator to integrate said
  equations of motion so as to obtain calculations of said behavior of said molecule.
- The method of claim 1 wherein said analytic Jacobian is derived from an analytic Jacobian of the Residual Form of the equations of motion.
  - 3. The method of claim 2 wherein said analytic Jacobian J comprises

$$J = \begin{pmatrix} \frac{\partial \dot{q}}{\partial q} & \frac{\partial \dot{q}}{\partial u} \\ \frac{\partial \dot{u}}{\partial q} & \frac{\partial \dot{u}}{\partial u} \end{pmatrix} \triangleq \begin{pmatrix} J_{qq} & J_{qu} \\ J_{uq} & J_{uu} \end{pmatrix}; \text{ and }$$

$$J_{qq} = \frac{\partial \dot{q}}{\partial q} = \frac{\partial \left(Wu\right)}{\partial q}$$
 and  $J_{qu} = \frac{\partial \dot{q}}{\partial u} = W$ 

$$J_{uq} = \frac{\partial \dot{u}}{\partial a} = -M^{-1} \frac{\partial \rho_u(q, u, z)}{\partial a} \quad \text{and} \quad J_{uu} = \frac{\partial \dot{u}}{\partial u} = -M^{-1} \frac{\partial \rho_u(q, u, z)}{\partial u}$$

where q are the generalized coordinates, u are the generalized speeds, W is a joint map matrix and M is the mass matrix and  $\rho_u$  is the dynamic residual of the equations of motion, and z is  $-M^{-1}\rho_u(q,u,0)$ .

- The method of claim 3 wherein said implicit integrator selecting step comprises an L-stable integrator.
- A method of simulating the behavior of a physical system, comprising modeling said physical system with a torsion angle, rigid multibody model, said model having equations of motion; and

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integrating said equations of motion with an implicit integrator; said implicit integrator having an analytic Jacobian to obtain calculations of said behavior of said physical system.

- The method of claim 5 wherein said analytic Jacobian is derived from
   an analytic Jacobian of the Residual Form of the equations of motion.
  - 7. The method of claim 6 wherein said analytic Jacobian J comprises

$$J = \begin{pmatrix} \frac{\partial \dot{q}}{\partial q} & \frac{\partial \dot{q}}{\partial u} \\ \frac{\partial \dot{u}}{\partial q} & \frac{\partial \dot{u}}{\partial u} \end{pmatrix} \triangleq \begin{pmatrix} J_{qq} & J_{qu} \\ J_{uq} & J_{uu} \end{pmatrix}; \text{ and }$$

$$J_{qq} = \frac{\partial \dot{q}}{\partial q} = \frac{\partial \left(Wu\right)}{\partial q} \quad \text{and} \quad J_{qu} = \frac{\partial \dot{q}}{\partial u} = W$$

$$J_{uq} = \frac{\partial \dot{u}}{\partial q} = -M^{-1} \frac{\partial \rho_u(q,u,z)}{\partial q} \quad \text{and} \quad J_{uu} = \frac{\partial \dot{u}}{\partial u} = -M^{-1} \frac{\partial \rho_u(q,u,z)}{\partial u}$$

where q are the generalized coordinates, u are the generalized speed, W is a joint map matrix and M is the mass matrix and  $\rho_u$  is the dynamic residual of the equations of motion, and z is  $-M^{-1}\rho_u(q,u,0)$ .

- The method of claim 7 wherein said implicit integrator comprises an L-stable integrator.
- 15 9. Computer code for simulating the behavior of a molecule, said code comprising

a first module for a torsion angle, rigid multibody model of said molecule, said model having equations of motion; and

- a second module for an implicit integrator to integrate said equations of motion with an analytic Jacobian to obtain calculations of said behavior of said molecule.
  - 10. The computer code of claim 9 wherein said analytic Jacobian is derived from an analytic Jacobian of the Residual Form of the equations of motion.

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 $11. \qquad \mbox{The computer code of claim 10 wherein said analytic Jacobian J} \label{eq:comprises}$ 

$$J = \begin{pmatrix} \frac{\partial \dot{q}}{\partial q} & \frac{\partial \dot{q}}{\partial u} \\ \frac{\partial \dot{u}}{\partial a} & \frac{\partial \dot{u}}{\partial u} \end{pmatrix} \triangleq \begin{pmatrix} J_{qq} & J_{qu} \\ J_{uq} & J_{uu} \end{pmatrix}; \text{ and }$$

$$J_{qq} = \frac{\partial \dot{q}}{\partial q} = \frac{\partial \left(Wu\right)}{\partial q}$$
 and  $J_{qu} = \frac{\partial \dot{q}}{\partial u} = W$ 

$$J_{uq} = \frac{\partial \dot{u}}{\partial q} = -M^{-1} \frac{\partial \rho_u(q, u, z)}{\partial q} \quad \text{and} \quad J_{uu} = \frac{\partial \dot{u}}{\partial u} = -M^{-1} \frac{\partial \rho_u(q, u, z)}{\partial u}$$

where q are the generalized coordinates, u are the generalized speed, W is a joint map matrix and M is the mass matrix and  $\rho_u$  is the dynamic residual of the equations of motion, and z is  $-M^{-1}\rho_u(q,u,0)$ .

- The computer code of claim 11 wherein said implicit integrator comprises an L-stable integrator.
- Computer code for simulating the behavior of a physical system, said code comprising
- a first module for a torsion angle, rigid multibody model of said system, said model having equations of motion; and
- a second module for an implicit integrator to integrate said equations of motion with an analytic Jacobian to obtain calculations of said behavior of said system.
- 14. The computer code of claim 13 wherein said analytic Jacobian is derived from an analytic Jacobian of the Residual Form of the equations of motion.
- ${\rm 15.} \qquad {\rm The\ computer\ code\ of\ claim\ 14\ wherein\ said\ analytic\ Jacobian\ J}$   ${\rm 20} \qquad {\rm comprises}$

$$\begin{split} J = & \left( \frac{\partial \dot{q}}{\partial q} \, \frac{\partial \dot{q}}{\partial u} \, \right) \triangleq \begin{pmatrix} J_{qq} & J_{qu} \\ J_{uq} & \frac{\partial \dot{u}}{\partial q} & \frac{\partial \dot{u}}{\partial u} \end{pmatrix}; \text{ and} \\ \\ J_{qq} = & \frac{\partial \dot{q}}{\partial q} = & \frac{\partial (Wu)}{\partial q} \quad \text{and} \quad J_{qu} = & \frac{\partial \dot{q}}{\partial u} = W \end{split}$$

$$J_{uq} = \frac{\partial \dot{u}}{\partial q} = -M^{-1} \frac{\partial \rho_u(q, u, z)}{\partial q} \quad \text{and} \quad J_{uu} = \frac{\partial \dot{u}}{\partial u} = -M^{-1} \frac{\partial \rho_u(q, u, z)}{\partial u}$$

where q are the generalized coordinates, u are the generalized speed, W is a joint map matrix and M is the mass matrix and  $\rho_u$  is the dynamic residual of the equations of motion, and z is  $-M^{-1}\rho_s(q,u,0)$ .

 The computer code of claim 15 wherein said implicit integrator comprises an L-stable integrator.